

# Running the LMTO code

## A quick tutorial

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## Outline

- LDA calculation
- Estimation of U and J
- LDA+U calculation

## Technical details

- Realization of DFT method: Local Density Approximation in Tight-Binding Linearized Muffin-Tin formalism (TB-LMTO)
- Manuals for the TB-LMTO can be found in tb/OTHER/doc/
- Tested with **ifort** and **g95** compilers
- Configure makefile and copy the binaries to your local /bin
- To get the code ask tutor

## What do we need to know to get started?

- Crystal structure:
  - ▶ Lattice constants
  - ▶ Crystal symmetry
  - ▶ Translation vectors
  - ▶ Atomic positions
- Information about elements:
  - ▶ Atomic number
  - ▶ Configuration of valent shells
  - ▶ Initial guess of charge distribution

## What can we get?

- Total energy
- Density of states
- Charge and spin distributions
- Fermi surface
- Band structure along directions in k-space between high symmetry points
- Forces
- ...

## CoO

- CoO periclase (rock salt) structure;
  - ▶ Co has octahedral coordination of O;
  - ▶  $t_{2g}$  and  $e_g$  are separated in energy;
  - ▶  $t_{2g}$  and  $e_g$  are not hybridized;
- CoO is a  $d^7$  system;
- CoO is an antiferromagnetic charge-transfer insulator ( $T_N = 291K$ );

## Crystal structure parameters of CoO

Space group                     $Fm\bar{3}m$  (Number 225)  
Lattice constant                4.2615 atomic units  
Atomic coordinates:  
                                Co (0, 0, 0)  
                                O (0.5, 0.5, 0.5)

## Part I

# Calculation of a bandstructure within LDA

## Production of CTRL file

- make INIT file: change to your working directory and type *lm47.run lminit*

```
QUERY : Spacegroup symbol or number 225
```

```
Space group: Fm-3m      No.:225
```

```
Crystal system: cubic
```

```
Generators: I R4X R3D
```

```
QUERY : atomic-units? (else Angstrom)(DEFAULT=T) F
```

```
Now enter lattice parameters
```

```
QUERY : A :lattice parameter (in Angstrom)      4.2615
```

```
CTRLUC:          PLAT          ALAT=  8.05307  
    0.00000  0.50000  0.50000  
    0.50000  0.00000  0.50000  
    0.50000  0.50000  0.00000
```

```
QUERY : Label or nuclear charge  Co
```

```
QUERY : X = position of Co (DEFAULT=0. 0. 0.) 0.0 0.0 0.0
```

```
QUERY : Label or nuclear charge  O
```

```
QUERY : X = position of O (DEFAULT=0. 0. 0.) 0.5 0.5 0.5
```

```
QUERY : Label or nuclear charge  q
```

## Production of CTRL file

- determine atomic sphere radius:

*user@somehost > lm47.run lmhart*

- check atomic sphere overlap:

*user@somehost > lm47.run lmovl*

- try to insert empty spheres (and again check atomic sphere overlap):

*user@somehost > lm47.run lmes*

*user@somehost > lm47.runl movl*

- complete CTRL file:

set VERBOS parameter(CTRL file 3rd line) to 50

*user@somehost > lm47.run lmctl*

## **Important categories and tokens of CTRL file**

```
IO      VERBOS=50 OUTPUT=LOUT ERR=LERR
SYMGRP NGEN=3 GENGRP=I R4X R3D
        SPCGRP=Fm-3m USESYM=F
STRUC   ALAT=8.0530711
        PLAT=0.0 0.5 0.5
              0.5 0.0 0.5
              0.5 0.5 0.0 FIXLAT=T
OPTIONS NSPIN=1 REL=T CCOR=T NONLOC=F NRXC=1 NR MIX=2 CORDRD=F
        NITATOM=30 CHARGE=F FATBAND=F AFM=F SEWALD=F FS=F
        CARTESIAN=T WRIBAS=F Q=---- LOCALCS=F GAMMA=F Zero_Ppar=F
CLASS    ATOM=Co Z=27 R=2.57891492 LMX=2 CONF=4 4 3 4 IDXDN=1 1 1
        IDMOD=0 0 0 RHO_print=0 0 0
        ATOM=O Z= 8 R=2.03070701 LMX=2 CONF=3 2 3 4 IDXDN=2 1 2
        IDMOD=0 0 0 RHO_print=0 0 0
SITE     ATOM=Co POS= 0.00 0.00 0.00
        ATOM=O POS= 0.50 0.50 0.50
        ATOM=E POS= 0.25 0.25 0.25
        ATOM=E POS=-0.25 -0.25 -0.25
```

## Important categories and tokens of CTRL file

```
START      NIT=30 BROY=T WC=-1 NMIX=1 BETA=0.5
FREE=F CNVG=0.00001 CNVGET=0.00001 BEGMOM=T CNTROL=T
EFERMI=-0.25 VMTZ=-0.75
ATOM=Co   P=4.66 4.41 3.83
          Q=0.6 0.0 0.0
          0.8 0.0 0.0
          7.6 0.0 0.0
enu       ==-0.452 -0.282 -0.194
c         ==-0.267  0.830 -0.141
sqrdel=0.514 0.642 0.236
p         =0.033 0.019 1.390
gamma    = 0.558 0.252 -0.003
SCELL     PLAT=0.0 0.5 0.5
          0.5 0.0 0.5
          0.5 0.5 0.0 EQUIV=T
UCORREC   Ucorr=F unitsEV=T DOSp=F Classes=1 N_avr=F LSDA+U=T
CLASS=Co L=2 Uvalue=0 Jvalue=0
MixVCL=1 add_Hole=0 U_on_p0=F
FANTOMS   Constrn=F Leip=F HMLT=F Sabbath=F
```

## Changes in CTRL before start of self-consistency loop

```
UCORREC Ucorr=T unitsEV=T DOSp=F Classes=1 N_avr=F LSDA+U=T  
CLASS=Co L=2 Uvalue=0 Jvalue=0
```

**Keep INIT and CTRL files (cp CTRL CTRL.start)  
and remove other files from working directory.**

### Start of self-consistency loop:

*user@somehost > lm47.run lm &*

## Trace the process of self-consistency

- how many iterations are finished already:  
*grep OF LOUT*
- value of the Fermi energy:  
*grep 'S: F' LOUT*
- density of states at the Fermi level:  
*grep Den LOUT*
- difference in total energy:  
*grep DETOT LOUT*
- when the calculation is self consistent?

Jolly good show! You converged to DETOT=0.00000100

## Information obtained from LDA calculation

- Density of states at the Fermi energy

*grep Den LOUT*

BANDWT: Density of states at E\_f: N(E\_f) = 40.432768

- total energy of the system is

*grep OF LOUT*

ITER 1 OUT OF 30: MAG MOM= 0.00000000 ETOT= -2933.01524920

- occupancy of 3d-orbital of Co

*grep -5 maj LOUT*

===== LSDA+U calculation =====

U=0.00000 and J=0.00000 for d orbitals of Co

OCCUPATIONS MATRIX :

----> majority spin diagonal occupancy 7.59865 <----

1.90619756 -0.00000000 0.00000000 0.00000000 0.00000000

-0.00000000 1.90619756 -0.00000000 0.00000000 -0.00000000

0.00000000 -0.00000000 0.94002958 -0.00000000 0.00000000

0.00000000 0.00000000 -0.00000000 1.90619756 0.00000000

0.00000000 -0.00000000 0.00000000 0.00000000 0.94002958

## Calculation of bands (spaghetti)

- edit the CTRL file

```
OPTIONS    NSPIN=1 REL=T CCOR=T NONLOC=F NRXC=1 NRMIX=2 CORDRD=F  
          NITATOM=30 CHARGE=F FATBAND=T AFM=F SEWALD=F FS=F  
          CARTESIAN=T WRIBAS=F Q=----- LOCALCS=F GAMMA=F Zero_Ppar=F
```

- information about symmetry lines is in category SYML

```
SYML      NQ=35 Q1=0.50 0.50 0.50 LAB1=L  
          Q2=0.00 0.00 0.00 LAB2=G  
          NQ=40 Q1=0.00 0.00 0.00 LAB1=G  
          Q2=0.00 1.00 0.00 LAB2=X  
          NQ=20 Q1=0.00 1.00 0.00 LAB1=X  
          Q2=0.50 1.00 0.00 LAB2=W  
          NQ=30 Q1=0.50 1.00 0.00 LAB1=W  
          Q2=0.50 0.50 0.50 LAB2=L  
          NQ=25 Q1=0.50 0.50 0.50 LAB1=L  
          Q2=0.00 0.75 0.75 LAB2=K  
          NQ=45 Q1=0.00 0.75 0.75 LAB1=K  
          Q2=0.00 0.00 0.00 LAB2=G
```

- execute the command

*user@somehost > lm47.run lmbnd*

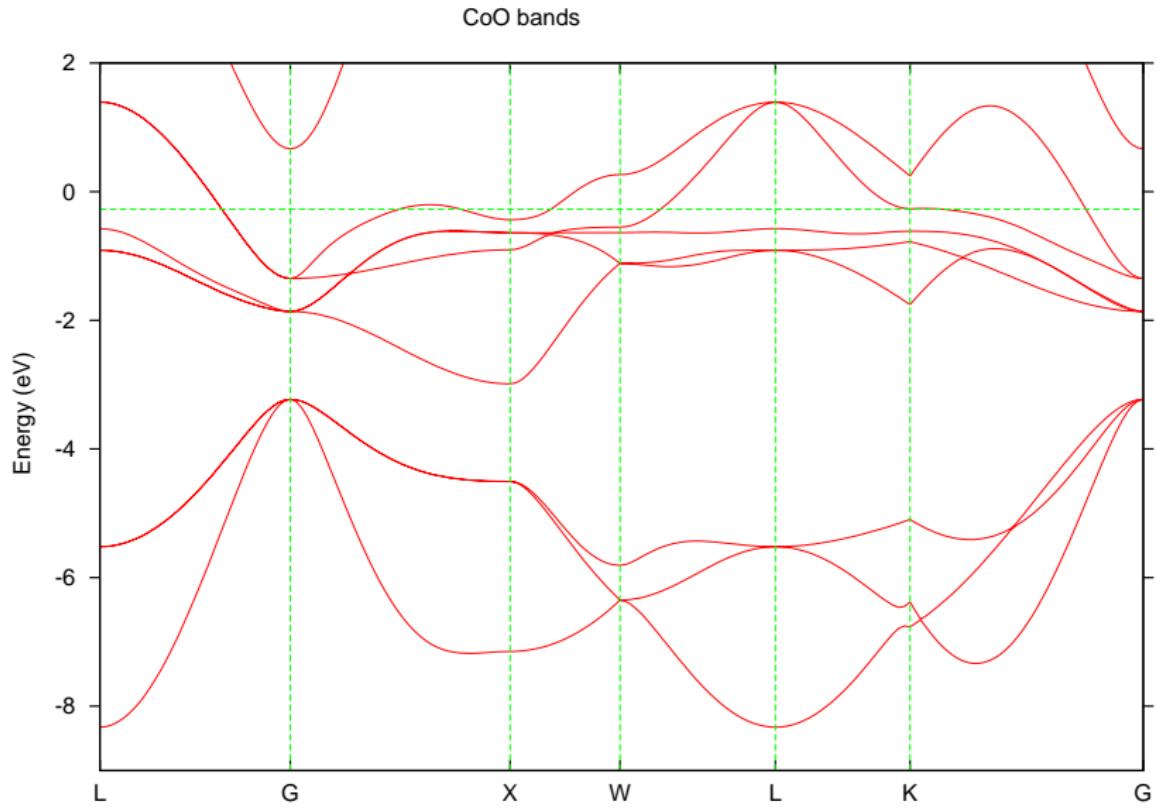
- run gnubnd.run command to prepare files for plotting the bands

*user@somehost > gnubnd.run*

(it is interactive) and answer some questions:

```
enter title
CoO bands
  energies in Rydberg (f) or eV (t) ? (default is Rydberg)
t
  energies relative to EF (t)? (default is f)
f
  landscape plot (t) ? (default t)
t
  energies connected by lines (t)? (default t)
t
  show E_nu's ? (default t)
f
  plot orbital character(t)? (default f)
f
Bands= 14 Fermi Energy= -0.2724 Lattice const.= 8.053 Spins= 1
ebot= -8.325    etop= 40.089    efermi= -0.272    nkp= 195    nline= 6
default emin and emax = -9.000 41.000
enter emin, emax
-9 2
```

- visualize the band structure (using gnuplot)  
*user@somehost > gnuplot < BNDS.GNU*
- now you have the file *bnds.ps*
- View it!



- Rename this file, for example :

```
mv bnds.ps all.bnds.ps
```

---

How to determine contributions from different states to the band structure? Let us plot orbital projected bands or "fat bands" for the Co *d* states.

- run *gnubnd.run* command again and answer some questions:

```
enter title
Co-3d bands of Co0
    energies in Rydberg (f) or eV (t) ? (default is Rydberg)
t
    energies relative to EF (t)? (default is f)
f
    landscape plot (t) ? (default t)
t
    energies connected by lines (t)? (default t)
t
    show E_nu's ? (default t)
f
    plot orbital character(t)? (default f)
t
    Change coordinate system? If so enter Euler angles:
    alpha, beta, gamma(units of Pi). If nochange: enter '/'
/
    no coordinate transformation!
    Do you want to make a compound orbital? (default f)
f
    Enter orbital character to be plotted as "fatbands"
```

First select classes from: Co    O    E

Co

For each selected atom specify orbital number from list  
NB! Orbitals are in the new coordinate system!

s y z x xy yz  $3z^2-1$  xz  $x^2-y^2$   $y(3x^2-y^2)$  xyz  
1 2 3 4 5 6 7 8 9 10 11  
 $y(5z^2-1)$   $z(5z^2-3)$   $x(5z^2-1)$   $z(x^2-y^2)$   $x(3y^2-x^2)$   
12 13 14 15 16

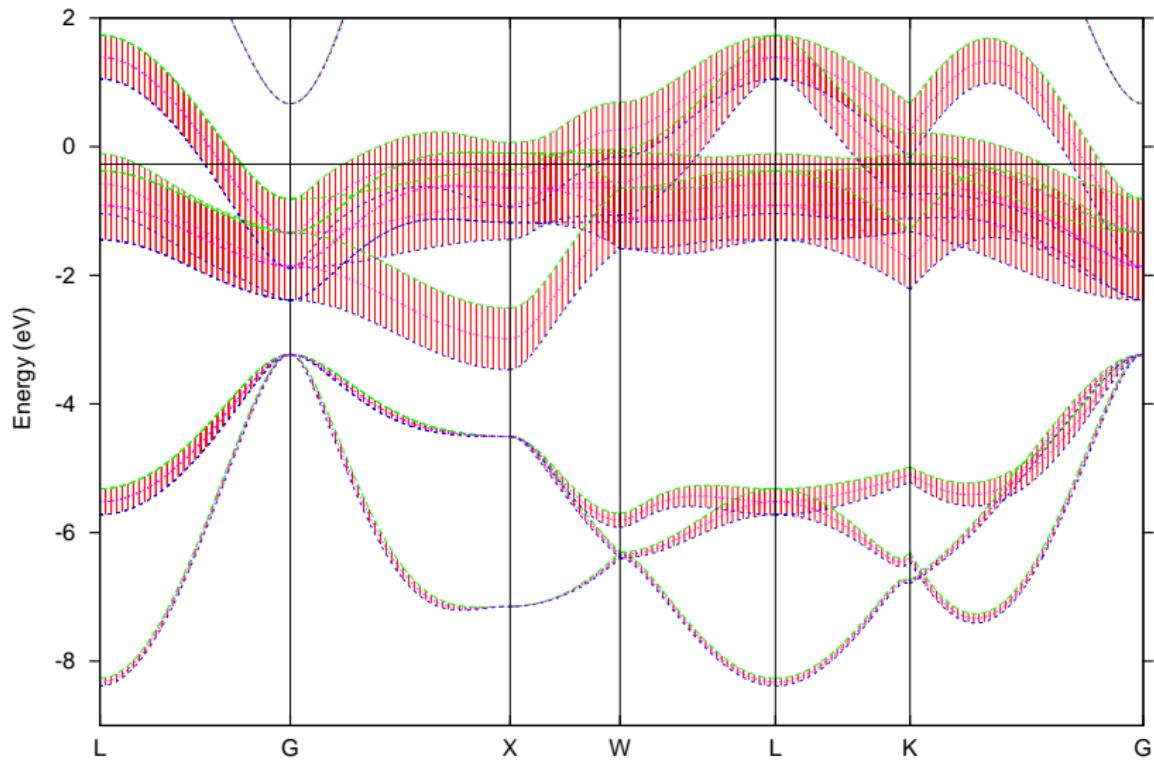
Co number 1 enter number(s) followed by "/":

5 6 7 8 9 /

Bands= 14 Fermi Energy= -0.2724 Lattice const.= 8.053 Spins= 1  
ebot= -8.325 etop= 40.089 efermi= -0.272 nkp= 195 nline= 6  
default emin and emax = -9.000 41.000  
enter emin, emax  
-9 2  
max. width 0.550000

- visualize the bands with gnuplot  
*user@somehost > gnuplot < BNDS.GNU*
- View bnds.ps file. The more fat is the band – the larger is contribution of Co 3d states

### Co-3d bands of CoO



- Now lets do same analysis for the O-2p contributions...

```
enter title
O-2p bands of CoO
  energies in Rydberg (f) or eV (t) ? (default is Rydberg)
t
  energies relative to EF (t)? (default is f)
f
  landscape plot (t) ? (default t)
t
  energies connected by lines (t)? (default t)
t
  show E_nu's ? (default t)
f
  plot orbital character(t)? (default f)
t
  Change coordinate system? If so enter Euler angles:
  alpha, beta, gamma(units of Pi). If nochange: enter '/'
/
  no coordinate transformation!
  Do you want to make a compound orbital? (default f)
f
```

Enter orbital character to be plotted as "fatbands"

First select classes from: Co    O    E

O

For each selected atom specify orbital number from list

NB! Orbitals are in the new coordinate system!

s    y    z    x    xy    yz     $3z^2-1$     xz     $x^2-y^2$      $y(3x^2-y^2)$     xyz  
1    2    3    4    5    6    7    8    9                        10                    11

$y(5z^2-1)$      $z(5z^2-3)$      $x(5z^2-1)$      $z(x^2-y^2)$      $x(3y^2-x^2)$   
12                    13                    14                    15                    16

0    number    1 enter number(s) followed by "/":

2 3 4 /

Bands= 14 Fermi Energy= -0.2724 Lattice const.= 8.053 Spins= 1

eboot= -8.325 etop= 40.089 efermi= -0.272 nkp= 195 nline= 6

default emin and emax = -9.000 41.000

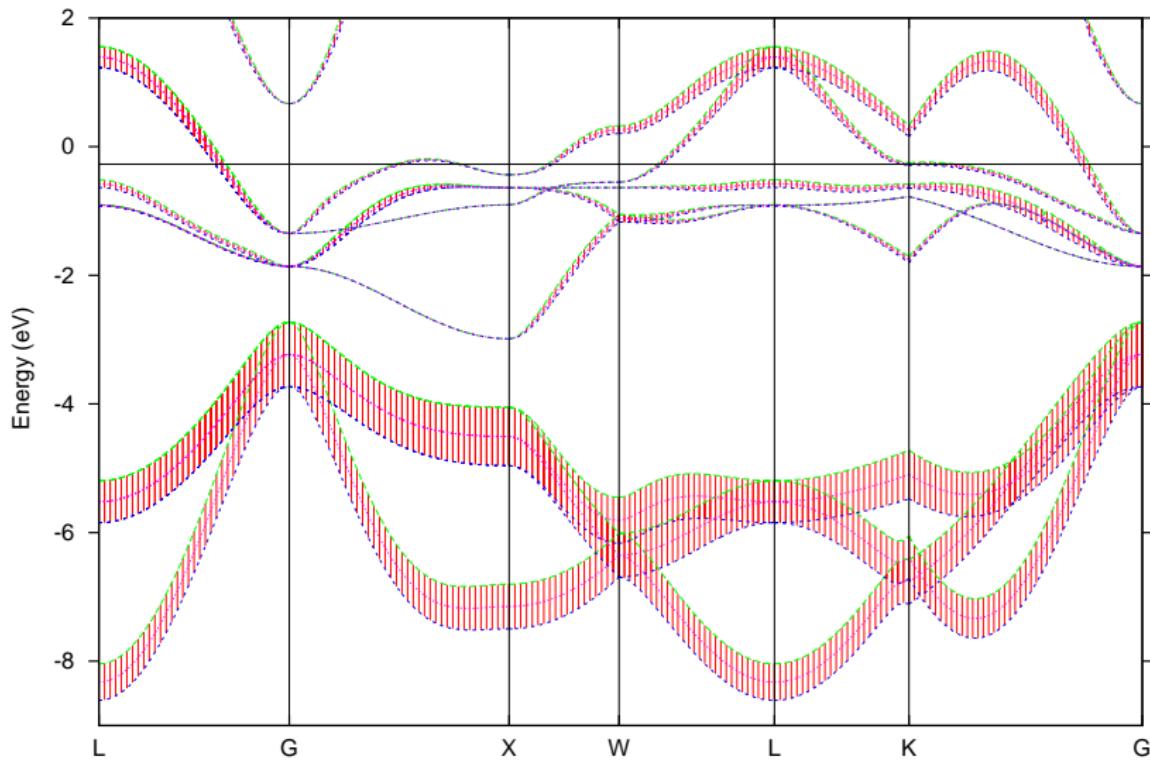
enter emin, emax

-9 2

max. width 0.550000

- ...and plot the bands

### O-2p bands of CoO



## Calculation of density of states (DOS)

- edit the CTRL file

```
UCORREC Ucorr=T unitsEV=T DOSp=T Classes=1 dblUset=F LSDA+U=T  
CLASS=Co L=2 Uvalue=0 Jvalue=0
```

- execute the command

```
user@somehost > lm47.run lmdos
```

- run the command to prepare files for plotting the total DOS

```
user@somehost > gnudos.run
```

and answer some questions...

Differential (f, default) or integer (t) DOS ?

f

energies in Rydberg (f) or eV (t)? (default is Rydberg)

t

energies relative to EF (t)? (default is f)

f

emin,emax= -9.5226 40.8188, nopts= 801, nd= 9 efermi= -0.2724

classes are: Co 0 E

l's are: s p d

Enter class1-l1, class2-l2, ... to be added to DOS.

Examples: all (default) s p Co-d E-s

/

Take: Co-s Co-p Co-d O-s O-p O-d E-s E-p  
E-d

Now enter weights for partial DOS (default = 1.0, 1.0, ...)

A weight of 1.0 for each partial DOS gives the correct total DOS.

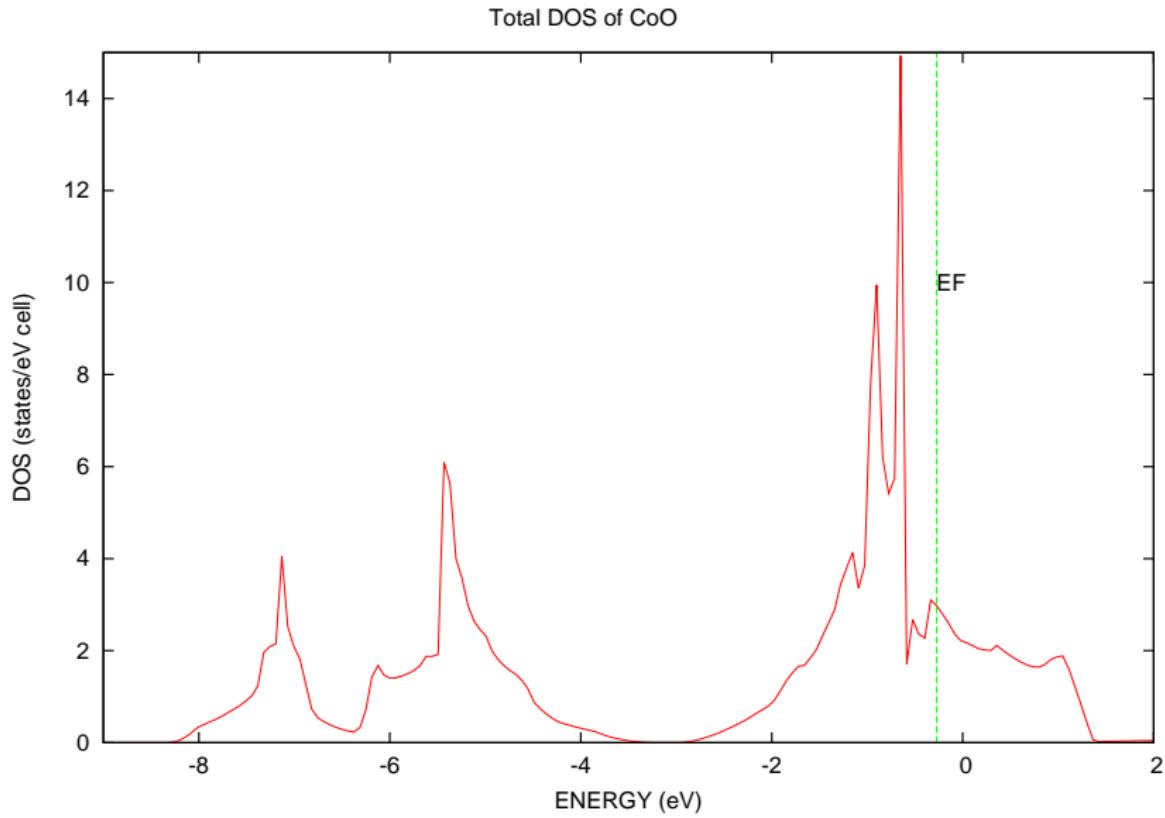
/

emin , emax = -9.523 40.819

if desired, enter new emin, emax, / for default

-9 2

- and plot the result:



- Rename the file dos.ps

```
mv dos.ps total.dos.ps
```

---

How to plot  $l$ -projected densities of states (partial DOS)?  
Let us plot partial DOS for Co  $d$  states.

- run again the command to prepare files for plotting the DOS  
*user@somehost > gnudos.run*  
and answer some questions(part of the dialog is skipped):

```
energies relative to EF (t)? (default is f)
f
emin,emax= -9.5226 40.8188, nopts= 801, nd= 9 efermi= -0.2724

classes are: Co 0 E
l's are: s p d
```

Enter class1-l1, class2-l2, ... to be added to DOS.

Examples: all (default) s p Co-d E-s

Co-d

Take: Co-d

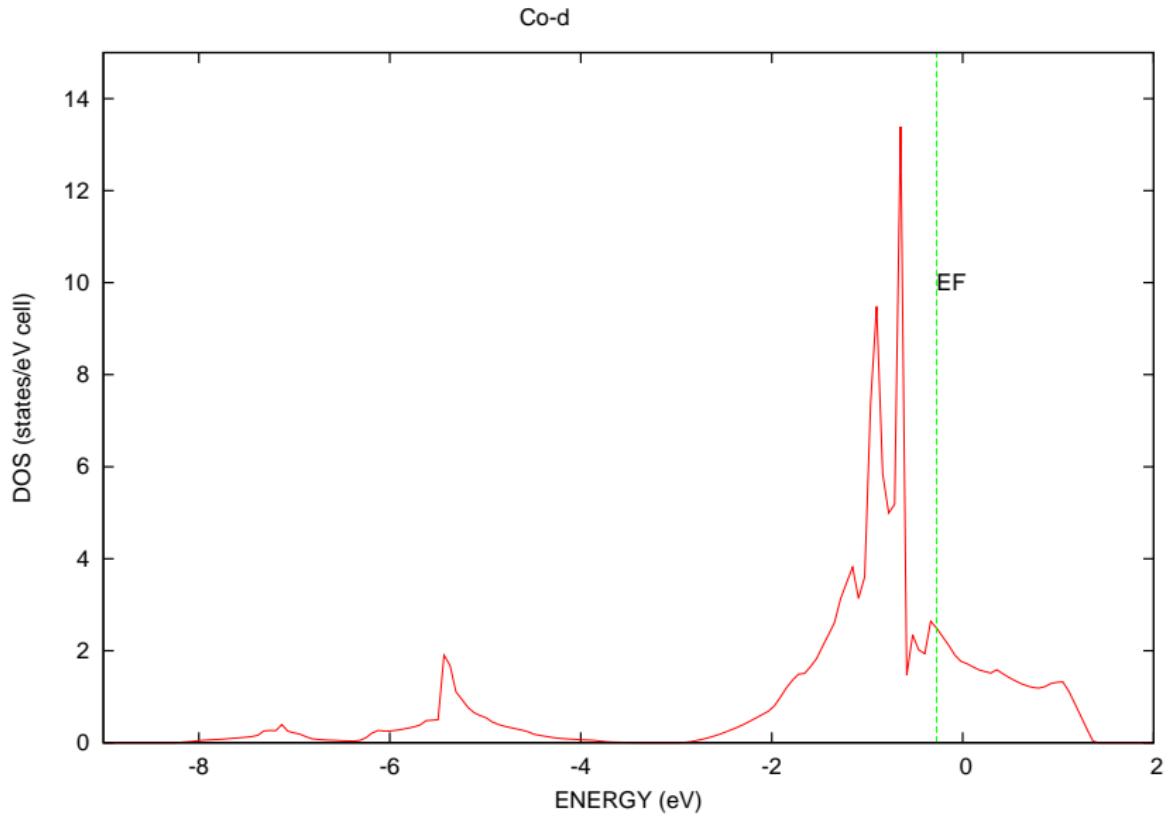
Now enter weights for partial DOS (default = 1.0, 1.0, ...)

A weight of 1.0 for each partial DOS gives the correct total DOS.

/

```
emin , emax = -9.523 40.819
if desired, enter new emin, emax, / for default
-9 2
```

```
dosmin, dosmax =.0 13.392
if desired, enter new dosmin, dosmax, / for default
/
```



## How to plot $m$ projected densities of states for Co (DOS for $xy$ , $yz$ , $3z^2 - r^2$ , $zx$ , $x^2 - y^2$ orbitals)?

- run the other command to prepare files for plotting the DOS

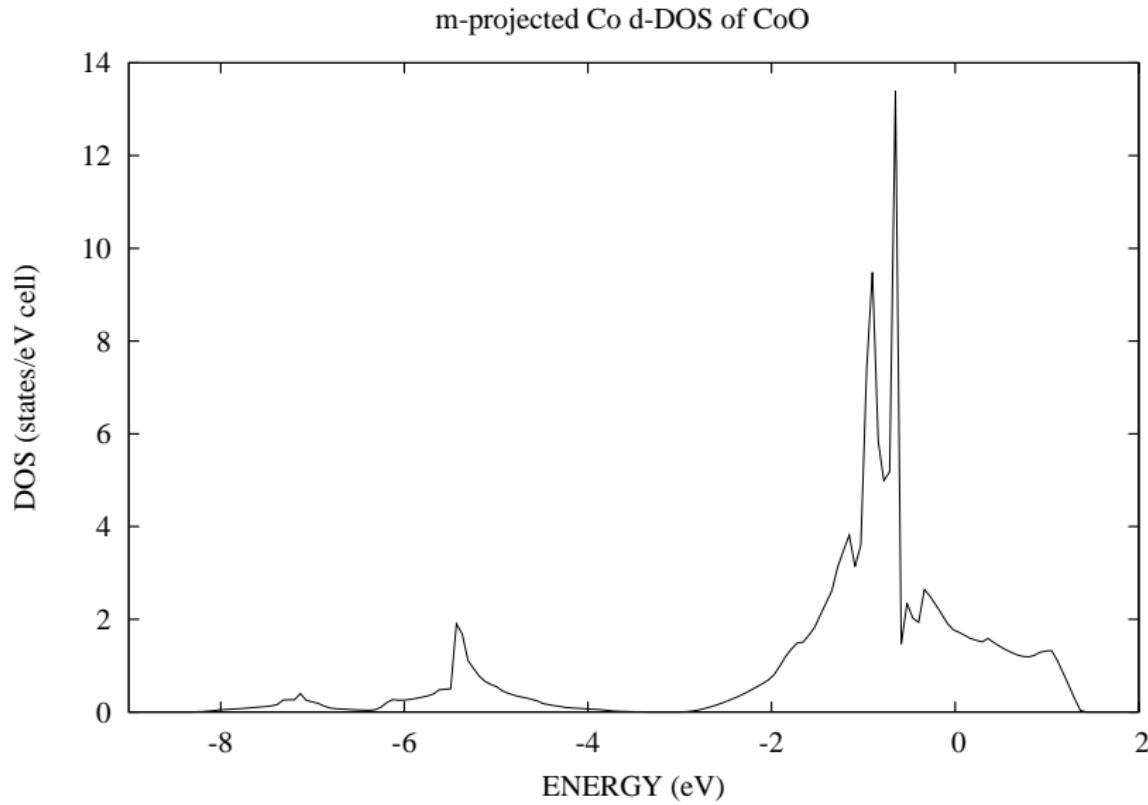
*gnudosp.run*

and answer some questions(part of the dialog is skipped):

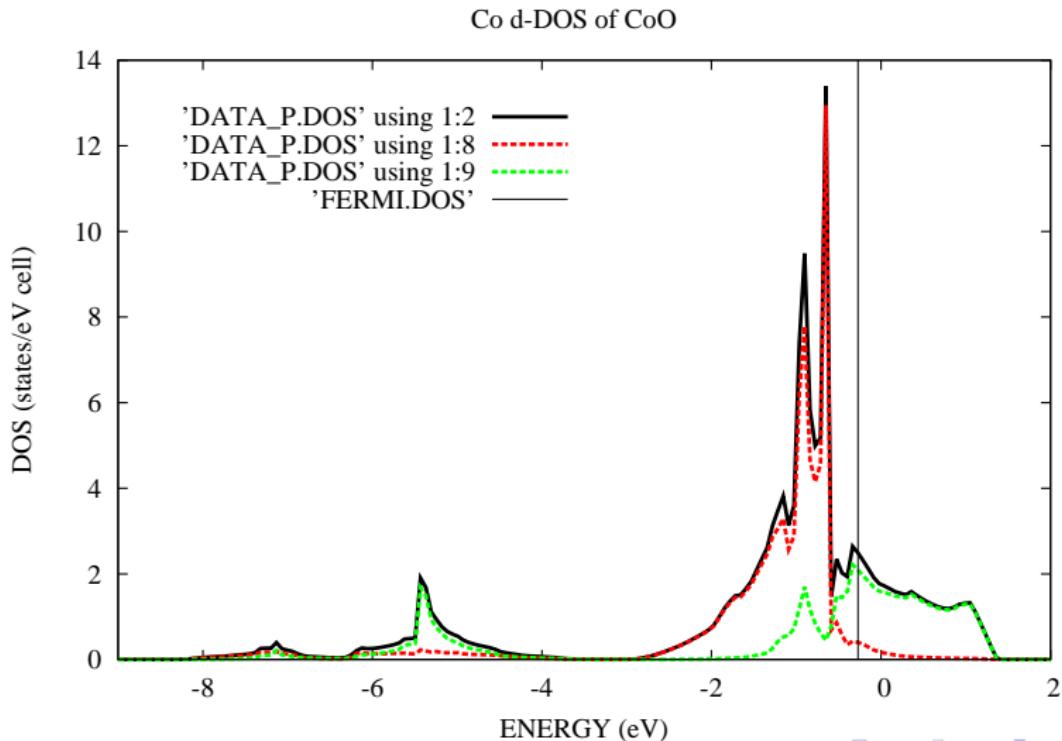
```
energies relative to EF (t)? (default is f)
f
Atom number?
1
emin,emax= -9.5226 40.8188, npts= 801    efermi= -0.2724
Do you need rotation? (default is (f))
f

Enter title
m-projected Co d-DOS of Co0
Print DOS file in matrix form? (default - f)
f
```

- visualize the result using gnuplot: *gnuplot DOSP.GNU*



- orbitally resolved densities of states for Co atom are in \DATA\_P.DOS file.  
The columns contain Energy, Total Co-d,  $xy$ ,  $yz$ ,  $3z^2 - r^2$ ,  $zx$ ,  $x^2 - y^2$ ,  
 $t_{2g}$ ,  $e_g$  orbitals, respectively



## Part II

### Calculation of U and J parameters

## Calculation of on-site Coulomb interaction parameter $U$ with the use of *constrain* method

- $U = \delta\epsilon_{3d}/\delta n_{3d}$ ,  
where  $\epsilon_{3d}$  is the energy of  $3d$  band  
and  $n_{3d}$  is the occupancy of  $3d$  shell
- $\epsilon_{3d}$  corresponds to  $c$  parameter (center of gravity of the occupied band) of the LMTO method

see also *Pickett W.E., Erwin S.C. and Ethridge E.C.* Reformulation of the LDA + U method for a local-orbital basis // Phys. Rev. B. 1998. V. 58. N 3. P. 1201–1209.

## Step 1.

- Take the CTRL file from converged LDA calculation
- Make supercell of CoO which contains four Co atoms.  
Open the CTRL file and edit SCELL category:

```
SCELL      PLAT=1  0  0
           0  1  0
           0  0  1 EQUIV=T
```

- run the command to produce supercell  
*user@somehost > lm47.run lmscell*
- View new CTRL file! Now it contains four initial cells  
Note: there are still 2 classes of atoms: Co and O.

## Step 2.

- Make two Co atoms non-equivalent:

```
CLASS      ATOM=Co1 Z=27 R=2.57790832 LMX=2 CONF=4 4 3 4 IDXDN=1 1 1      <-
IDMOD=0 0 0 RHO_print=0 0 0
ATOM=Co2 Z=27 R=2.57790832 LMX=2 CONF=4 4 3 4 IDXDN=1 1 1      <-
IDMOD=0 0 0 RHO_print=0 0 0
ATOM=O   Z= 8 R=2.03007195 LMX=2 CONF=3 2 3 4 IDXDN=2 1 2
IDMOD=0 0 0 RHO_print=0 0 0
ATOM=E   Z= 0 R=1.41271966 LMX=1 CONF=1 2 3 4 IDXDN=1 2
IDMOD=0 0 RHO_print=0 0
SITE      ATOM=Co1 POS= 0.00 0.00 0.00      <-
ATOM=Co2 POS= 0.50 0.50 0.00      <-
ATOM=Co2 POS= 0.50 -0.00 0.50      <-
ATOM=Co2 POS= 0.00 0.50 0.50      <-
...

```

- and delete all lines starting from SCALE category

- run the command to produce new CTRL file  
*user@somehost > lm47.run lmctl*
- View the CTRL file! Now It contains two classes of Co
- All the O atoms we will consider as belonging to the same class. This assumption will stabilize the procedure of self-consistency.
- Edit the CTRL file again. Be accurate!
- Edit SYMGRP category:

SYMGRP NGEN=3 GENGRP=I R4X R3D  
SPCGRP=Pm-3m USESYM=T

- Change CLASS category:

```
CLASS      ATOM=Co1 Z=27 R=2.57790832 LMX=2 CONF=4 4 3 4 IDXDN=1 1 1
           IDMOD=0 0 2 RHO_print=0 0 0 <-
           ATOM=Co2 Z=27 R=2.57790832 LMX=2 CONF=4 4 3 4 IDXDN=1 1 1
           IDMOD=0 0 2 RHO_print=0 0 0 <-
           ATOM=O   Z= 8 R=2.03007195 LMX=2 CONF=3 2 3 4 IDXDN=2 1 2
           IDMOD=0 0 0 RHO_print=0 0 0
           ATOM=E   Z= 0 R=1.41271966 LMX=1 CONF=1 2 3 4 IDXDN=1 2
           IDMOD=0 0 RHO_print=0 0
           ATOM=O1  Z= 8 R=2.03007195 LMX=2 CONF=3 2 3 4 IDXDN=2 1 2
           IDMOD=0 0 0 RHO_print=0 0 0
```

- Change START directory and keep only first three lines

```
START     NIT=50 BROY=F WC=-1 NMIX=0 BETA=0.01
          FREE=F CNVG=0.00001 CNVGET=0.00001 BEGMOM=T CNTROL=T
          EFERMI=-0.0191586 VMTZ=-0.6712252
```

- Edit UCORREC and FANTOMS categories

```
UCORREC Ucorr=T unitsEV=T DOSp=F Classes=2 N_avr=F LSDA+U=T
          CLASS=Co1 L=2 Uvalue=0 Jvalue=0
          CLASS=Co2 L=2 Uvalue=0 Jvalue=0
          MixVCL=1 add_Hole=0 U_on_p0=F
FANTOMS Constrn=T Leip=F HMLT=F Sabbath=F
```

- Complete the CTRL file

*user@somehost > lm47.run lmctl*

- Now we want to enforce a difference in occupancy of the Co 3d states. Edit the CPOC file in the working directory so that it looks like this:

```

POTCOR: Hubbard correction 0.000000000000D+00
Co1 :
L=2:
-0.100000000000 0.000000000000 0.000000000000 0.000000000000 0.000000000000
0.000000000000 -0.100000000000 0.000000000000 0.000000000000 0.000000000000
0.000000000000 0.000000000000 -0.100000000000 0.000000000000 0.000000000000
0.000000000000 0.000000000000 0.000000000000 -0.100000000000 0.000000000000
0.000000000000 0.000000000000 0.000000000000 0.000000000000 -0.100000000000
double counting energy 0.000000000000D+00
-----
Co2 :
L=2:
0.100000000000 0.000000000000 0.000000000000 0.000000000000 0.000000000000
0.000000000000 0.100000000000 0.000000000000 0.000000000000 0.000000000000
0.000000000000 0.000000000000 0.100000000000 0.000000000000 0.000000000000
0.000000000000 0.000000000000 0.000000000000 0.100000000000 0.000000000000
0.000000000000 0.000000000000 0.000000000000 0.000000000000 0.100000000000
double counting energy 0.000000000000D+00
-----
0.100000000000 0.000000000000 0.000000000000 0.000000000000 0.000000000000
0.000000000000 0.100000000000 0.000000000000 0.000000000000 0.000000000000
0.000000000000 0.000000000000 0.100000000000 0.000000000000 0.000000000000
0.000000000000 0.000000000000 0.000000000000 0.100000000000 0.000000000000
0.000000000000 0.000000000000 0.000000000000 0.000000000000 0.100000000000
double counting energy 0.000000000000D+00
-----
0.100000000000 0.000000000000 0.000000000000 0.000000000000 0.000000000000
0.000000000000 0.100000000000 0.000000000000 0.000000000000 0.000000000000
0.000000000000 0.000000000000 0.100000000000 0.000000000000 0.000000000000
0.000000000000 0.000000000000 0.000000000000 0.100000000000 0.000000000000
0.000000000000 0.000000000000 0.000000000000 0.000000000000 0.100000000000
double counting energy 0.000000000000D+00
-----
```

- Start self-consistency process  
`user@somehost > lm47.run lm`

- If self-consistency is not reached after NIT iterations, set BEGMOM=F in the CTRL file and re-run lm command

```
FREE=F CNVG=0.00001 CNVGET=0.00001 BEGMOM=F CNTROL=T
```

- Take information about the Co-3d occupations and energies from the CTRL file:

```
ATOM=Co1 P=4.59403291 4.30946740 3.89758362
```

```
Q= 0.31720885 -0.01265951 0.01045560
```

```
0.41085358 -0.01289696 0.00523537
```

```
7.77135744 -0.16171997 0.12034854
```

```
enu =-0.43667920 -0.40272434 0.01141031
```

```
c =-0.13286303 0.97122077 0.01141067
```

```
sqrdel=-0.50692113 0.64424814 0.23362663
```

```
p =0.03308971 0.01850979 1.53406627
```

```
gamma = 0.5613183 0.2586050 -0.0146474
```

```
ATOM=Co2 P=4.63462771 4.33167747 3.89758362
```

```
Q= 0.35097538 -0.01443908 0.01154048
```

```
0.44317633 -0.01329211 0.00494702
```

```
7.46800177 -0.13639201 0.11664946
```

```
enu =-0.45356273 -0.41468550 -0.16388059
```

```
c =-0.22228933 0.87212940 -0.16388027
```

```
sqrdel=-0.50235259 0.63684762 0.22186230
```

```
p =0.03570924 0.01953683 1.62240954
```

```
gamma = 0.55882812 0.25617514 -0.00895143
```

- Now let's calculate the local coulomb potential, taking into account that:

Co1:  $\epsilon_{3d}=0.011$  Ry,  $n_{3d}=7.771$

Co2:  $\epsilon_{3d}=-0.164$  Ry,  $n_{3d}=7.468$

$$U = \frac{\delta\epsilon}{\delta n} = \frac{0.175}{0.303} = \mathbf{0.578 \text{ Ry}} = \mathbf{7.855 \text{ eV}}$$

---

## Calculation of intraatomic exchange interaction parameter $J$ with the use of *constrain* method

- $J = |\delta\epsilon_{3d}^{\uparrow\downarrow}/\delta n_{3d}^{\uparrow\downarrow}|$ ,

where  $\delta\epsilon_{3d}^{\uparrow\downarrow}$  is the energy difference of majority and minority  $c$  parameters (centers of gravity) for  $3d$  bands:  $\delta\epsilon_{3d}^{\uparrow\downarrow} = \epsilon_{3d}^{\uparrow} - \epsilon_{3d}^{\downarrow}$

and  $\delta n_{3d}^{\uparrow\downarrow}$  is the difference in occupancy between majority and minority bands:  $\delta n_{3d}^{\uparrow\downarrow} = n_{3d}^{\uparrow} - n_{3d}^{\downarrow}$

- Take the CTRL file from converged LDA calculation
- Edit CTRL file:
  - ▶ in category IO set VERBOS=50
  - ▶ in category OPTIONS set NSPIN=2
  - ▶ in category PHANTOM set Constrn=T

- Edit CLASS category

```
CLASS      ATOM=Co Z=27 R=2.57790832 LMX=2 CONF=4 4 3 4 IDXDN=1 1 1  
          IDMOD=0 0 2 RHO_print=0 0 0
```

- Set Ucorr=T (category UCORREC)
- Erase all lines in START category except the first three and change the following tokens and parameters:

```
START      NIT=50 BROY=F WC=-1 NMIX=0 BETA=0.01
```

- complete the CTRL file

*user@somehost > lm47.run lmctl*

- Enforce the energy difference of the Co-3d states by changing diagonal elements in the CPOC file:

```
POTCOR: Hubbard correction 0.000000000000D+00
Co :
L=2:
-.1000000000000 0.0000000000000 0.0000000000000 0.0000000000000 0.0000000000000
0.0000000000000 -.1000000000000 0.0000000000000 0.0000000000000 0.0000000000000
0.0000000000000 0.0000000000000 -.1000000000000 0.0000000000000 0.0000000000000
0.0000000000000 0.0000000000000 0.0000000000000 -.1000000000000 0.0000000000000
0.0000000000000 0.0000000000000 0.0000000000000 0.0000000000000 -.1000000000000
double counting energy 0.000000000000D+00
0.1000000000000 0.0000000000000 0.0000000000000 0.0000000000000 0.0000000000000
0.0000000000000 0.1000000000000 0.0000000000000 0.0000000000000 0.0000000000000
0.0000000000000 0.0000000000000 0.1000000000000 0.0000000000000 0.0000000000000
0.0000000000000 0.0000000000000 0.0000000000000 0.1000000000000 0.0000000000000
0.0000000000000 0.0000000000000 0.0000000000000 0.0000000000000 0.1000000000000
double counting energy 0.000000000000D+00
```

---

- start self-consistency cycle

*user@somehost > lm47.run lm*

- If self-consistency is not reached after NIT iterations, set BEGMOM=F in the CTRL file and re-run lm command
- After self-consistency cycle is finished extract the Co-3d occupations and c-parameters from the CTRL file:

```

ATOM=Co  P=4.66735709 4.35922298 3.89758362
          4.63859420 4.34355043 3.89758362
Q= 0.19823045 -0.00453332 0.00795638
      0.25593771 -0.00222151 0.00910358
4.97008829 0.08880200 0.07352792
      0.17641215 -0.00642166 0.00449599
      0.23373375 -0.00677706 0.00286026
2.36087373 -0.14808511 0.06042935
enu   ==-0.40708807 -0.34743219 -0.25661916
      -0.41101015 -0.34841174 -0.07511793
c     ==-0.23620573  0.84901196 -0.25661886
      -0.18522640  0.90831806 -0.07511757

```

- Compute J:

$$J = \frac{\epsilon_{3d}^{\uparrow} - \epsilon_{3d}^{\downarrow}}{n_{3d}^{\uparrow} - n_{3d}^{\downarrow}} = \frac{0.257 - 0.075}{4.970 - 2.361} = \mathbf{0.0698 Ry} = \mathbf{0.949 eV}$$


---

## Part III

### Calculation of a bandstructure within LDA+U

- Take the CTRL file from the converged LDA calculation
- Edit SYMGRP category:

```
SYMGRP      NGEN=3 GENGRP=I R4X R3D
            SPCCGRP=Pm-3m USESYM=T
```

- Change CLASS and OPTIONS categories:

```
OPTIONS      NSPIN=2 REL=T CCOR=T NONLOC=F NRXC=1 NRMIX=2 CORDRD=F
            NITATOM=30 CHARGE=F FATBAND=F AFM=F SEWALD=F FS=F
            CARTESIAN=T WRIBAS=F Q=---- LOCALCS=F GAMMA=T Zero_Ppar=F
CLASS       ATOM=Co Z=27 R=2.57790832 LMX=2 CONF=4 4 3 4 IDXDN=1 1 1
            IDMOD=0 0 2 RHO_print=0 0 0
```

- Erase all lines in START category except the first three and change the following tokens and parameters:

```
START      NIT=50 BROY=F WC=-1 NMIX=0 BETA=0.01
```

- Enter the calculated values of U and J parameters to UCORREC category:

```
UCORREC    Ucorr=T unitsEV=T DOSp=F Classes=1 N_avr=F LSDA+U=F
            CLASS=Co L=2 Uvalue=7.86 Jvalue=0.95
```

- Complete the CTRL file using lmctl command

*user@somehost > lm47.run lmctl*

- Edit the POCO file inserting initial energy difference between spin-up and spin-down:

```
POTCOR:      Hubbard correction  0.000000000000D+00
Co   :
L=2:
  0.100000000000  0.000000000000  0.000000000000  0.000000000000  0.000000000000
  0.000000000000  0.100000000000  0.000000000000  0.000000000000  0.000000000000
  0.000000000000  0.000000000000  0.100000000000  0.000000000000  0.000000000000
  0.000000000000  0.000000000000  0.000000000000  0.100000000000  0.000000000000
  0.000000000000  0.000000000000  0.000000000000  0.000000000000  0.100000000000
double counting energy  0.000000000000D+00
  -.100000000000  0.000000000000  0.000000000000  0.000000000000  0.000000000000
  0.000000000000  -.100000000000  0.000000000000  0.000000000000  0.000000000000
  0.000000000000  0.000000000000  -.100000000000  0.000000000000  0.000000000000
  0.000000000000  0.000000000000  0.000000000000  -.100000000000  0.000000000000
  0.000000000000  0.000000000000  0.000000000000  0.000000000000  -.100000000000
double counting energy  0.000000000000D+00
```

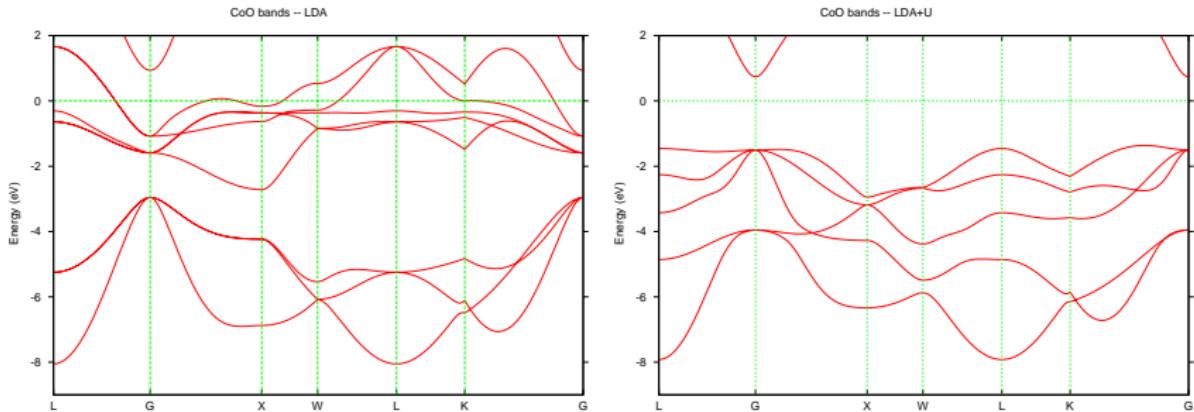
---

- run the self-consistency cycle

*user@somehost > lm47.run lm*

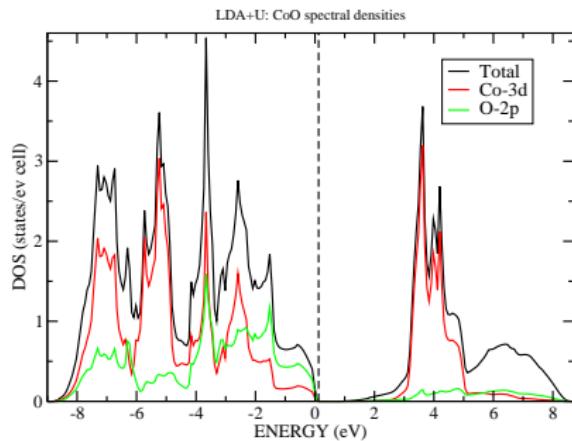
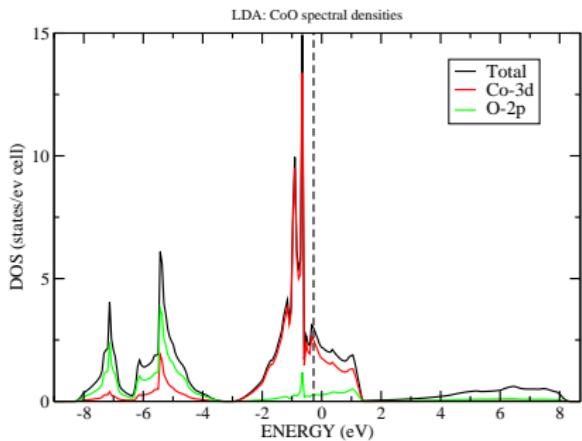
- By complete analogy with conducted LDA calculation one can get:
  - ▶ Total density of states
  - ▶ Element-resolved and orbitally resolved densities of states
  - ▶ Total band structure, its element and orbital contributions
- Next several slides demonstrate listed characteristics and properties for the case of CoO

## CoO: LDA vs LDA+U – band structure



- Qualitative improvement of LDA results
- The gap of experimentally observed magnitude

## CoO: LDA vs LDA+U – spectral densities



- Qualitative improvement of LDA results
- The gap of experimentally observed magnitude